PHYS 703 - Potential due to a sphere.

A conducting sphere is initially uncharged. At time t=0 it suddenly acquires a surface charge density $\sigma=\sigma_0\cos\theta$. Find the scalar potential and electric field on the positive z-axis outside the sphere as a function of time. Assume that $\vec{J}=0$ and thus $\vec{A}=0$ even though it gives rise to $\vec{B}=0$ for all times which we know can't be true.